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Second Semester B.E. Degree Examination, June 2012
Engineering Mathematics – II

Time: 3 hrs.

Max. Marks: 100

- Note: 1. Answer any FIVE full questions, choosing at least two from each part.**
2. Answer all objective type questions only on OMR sheet page 5 of the answer booklet.
3. Answer to objective type questions on sheets other than OMR will not be valued.

PART – A

- 1 a. Choose your answers for the following : (04 Marks)**
- i) The radius of curvature at a point (r, θ) of $r = ae^{\theta \cot \alpha}$ is
 A) $r \operatorname{cosec} \alpha$ B) $\operatorname{cosec} \alpha$ C) $\cot \alpha$ D) none of these
- ii) The radius of the circle of curvature is
 A) 1 B) $\frac{1}{\rho}$ C) ρ D) ρ^2
- iii) The value of C of the Lagrange's mean value theorem for $f(x) = \tan^{-1}x$ in $[0, 1]$ is
 A) 0.125 B) 0.523 C) $\pi/4$ D) $\pi/2$
- iv) Maclaurin's series expansion of $\sin x$ is
 A) $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots$ B) $1 - \frac{x^2}{2!} + \frac{x^3}{3!} - \dots$
 C) $x + \frac{x^3}{3!} + \dots$ D) $1 + x + \frac{x^2}{2} + \dots$
- b. Find the radius of curvature for the curve $y = a \log \sec(x/a)$ at any point (x, y) . (04 Marks)**
- c. State and prove Lagrange's mean value theorem. (06 Marks)**
- d. Expand $e^{\sin x}$, using Maclaurin's series upto the term containing x^4 . (06 Marks)**
- 2 a. Choose your answers for the following : (04 Marks)**
- i) $\lim_{x \rightarrow \infty} \sec\left(\frac{\pi}{2x}\right) \log x$ is equal to
 A) $\pi/2$ B) $2/\pi$ C) π D) $\pi/3$
- ii) The basic fundamental indeterminate forms are
 A) $\frac{0}{0}$ B) $\frac{\infty}{\infty}$ C) both A and B D) none of these
- iii) Find the critical point of the function $f(x, y) = \sin x + \sin y + \sin(x + y)$ is
 A) (1, 1) B) $(\pi/3, \pi/3)$ C) $(\pi/2, \pi/2)$ D) none of these
- iv) In a plane triangle ABC, the maximum value of $\cos A \cdot \cos B \cdot \cos C$ is
 A) $3/4$ B) $3/8$ C) $1/8$ D) $5/8$
- b. Evaluate $\lim_{x \rightarrow \pi/2} (2x \tan x - \pi \sec x)$. (04 Marks)**
- c. Expand $e^{ax} \sin y$ in powers of x and y as far as terms of 3rd degree. (06 Marks)**
- d. Show that the maximum value of $xy + a^3 \left(\frac{1}{x} + \frac{1}{y}\right)$ is $3a^2$. (06 Marks)**

3 a. Choose your answers for the following : (04 Marks)

i) $\int_0^2 \int_0^x (x+y) dx dy$ is equal to
 A) 3 B) 4 C) 5 D) none of these

ii) The volume of the cylinder with base radius 'a' and height 'h' is
 A) r^2h B) $\frac{2}{3}rh$ C) πr^2h D) none of these

iii) The value of $\beta(m, n)$ is
 A) $\int_0^\infty x^{m-1}(1-x)^{n-1} dx$ B) $\int_0^1 x^{m-1}(1-x)^x dx$
 C) $\int_0^1 x^{m-1}(1-x)^{n-1} dx$ D) none of these

iv) If n is a positive integer, then $\sqrt[n]{n+1}$ is equal to
 A) $n\sqrt[n]{n}$ B) $(n-1)\sqrt[n-1]{n-1}$ C) $n\sqrt[n+1]{n+1}$ D) n!

b. Calculate by double integration the volume generated by the revolution of the cardioid $r = a(1 - \cos \theta)$ about its axis. (04 Marks)

c. Evaluate $\int_0^1 \int_0^{\sqrt{1-x^2}} \int_0^{\sqrt{1-x^2-y^2}} xyz dx dy dz$. (06 Marks)

d. Show that $\int_0^{\pi/2} \sqrt{\sin \theta} d\theta \times \int_0^{\pi/2} \frac{1}{\sqrt{\sin \theta}} d\theta = \pi$. (06 Marks)

4 a. Choose your answers for the following : (04 Marks)

i) \vec{F} is said to be solenoidal, if
 A) $\int_c \vec{F} \cdot d\vec{r} = 0$ B) $\int_c \vec{F} \times d\vec{r} = 0$ C) $\vec{F} \times \vec{r} = 0$ D) none of these

ii) If $\vec{F} = 3xyi + y^2j$ and C is the curve, in the xy-plane, $y = x^2$ from (0, 0) to (1, 1), then $\int_C \vec{F} \cdot d\vec{r}$ is :

A) Constant B) Variable C) zero D) none of these

iii) Green's theorem in the plane is a special case of
 A) Gauss theorem B) Euler's theorem
 C) Baye's theorem D) Stoke's theorem.

iv) Stoke's theorem is a relation between
 A) a line integral and a surface integral B) a surface and volume integral
 C) two volume integrals D) a line and volume integral.

b. If $\vec{F} = 3xyi - y^2j$, evaluate $\int_C \vec{F} \cdot d\vec{r}$ along the curve $y = 2x^2$ in the xy-plane from (0, 0) to (1, 2). (04 Marks)

c. Evaluate, by Green's theorem, $\int_C (xy + y^2) dx + x^2 dy$, where C is bounded by $y = x$ and $y = x^2$. (06 Marks)

d. Prove that the cylindrical co-ordinates system is orthogonal. (06 Marks)

b. Find L.T of $e^{2t} \cos^2 t$. (04 Marks)

c. If $f(t)$ is a periodic function of period 'T', then show that $L\{f(t)\} = \frac{1}{1 - e^{-Ts}} \int_0^T e^{-st} f(t) dt$. (06 Marks)

d. Find $L\left\{\frac{e^{-at} - e^{-bt}}{t}\right\}$. (06 Marks)

8 a. Choose your answers for the following : (04 Marks)

i) Inverse Laplace transform of $\frac{1}{s^2 - a^2}$ is

A) $\frac{\text{Cos}at}{a}$ B) $\text{Sin}at$ C) $\text{Cos}hat$ D) $\frac{\text{Sin}hat}{a}$

ii) Inverse Laplace transform of $\frac{s+2}{s^2 - 4s + 13}$ is

A) $e^{-2t} \cos 3t + \frac{4}{3} e^{2t} \sin 3t$ B) $e^{2t} \sin 3t + \frac{3}{4} e^{-2t} \cos 3t$

C) $e^{2t} \sin 3t - \frac{4}{3} e^{-2t} \cos 3t$ D) $e^{2t} \cos 3t + \frac{4}{3} e^{2t} \sin 3t$

iii) Inverse Laplace transform of $\frac{s}{(s^2 + a^2)^2}$ is

A) $\frac{1}{2a} t \cos at$ B) $\frac{1}{2a} t \sin at$ C) $t \cos^2 at$ D) $\frac{t}{2} \sin at$

iv) $L^{-1}\left\{\frac{1}{s^n}\right\}$ is possible only when n is

A) $n > 1$ B) $n \geq -1$ C) $n = 1, 2, \dots$ D) $n < 1$.

b. Find the $L^{-1}\left\{\frac{s^2 - 2s + 1}{s^3}\right\}$. (04 Marks)

c. Find $L^{-1}\left\{\frac{3s + 7}{s^2 - 2s - 3}\right\}$. (06 Marks)

d. Applying L.T method, solve $x'' - 2x' + x = e^{2t}$ given that $x(0) = 0$ and $x'(0) = -1$. (06 Marks)

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